

Example 2. A nut is falling at a rate of -5m/s . If gravity accelerates the nut at a rate of -9.8m/s^2 , what will be the velocity of the nut after 6 more seconds?

$$-9.8\text{m/s}^2$$

$$V_{x0} = -5\text{m/s}$$

$$a = -9.8\text{m/s}^2$$

$$t = 6\text{s}$$

$$V_x = ?$$

$$V_x = V_{x0} + at$$

$$V_x = -5\text{m/s} + (-9.8\text{m/s}^2)(6\text{s})$$

$$V_x = -5\text{m/s} - 58.8\text{m/s} = -63.8\text{m/s}$$

1. A grouse takes off from the 8 yard line of a football field and travels to the 40 yard line over a time of 8 seconds. What is its average velocity?

$$\Delta x = 32\text{yards}$$

$$\Delta t = 8\text{s}$$

$$\bar{v} = \frac{\Delta x}{\Delta t} = \frac{32\text{yards}}{8\text{sec}} = 4\text{yards/sec}$$

2. How long will it take you to drive 200 miles if you have a velocity of 60mph?

$$\Delta x = 200\text{miles}$$

$$\bar{v} = 60\text{mph} = \frac{60\text{miles}}{\text{hour}}$$

$$\bar{v} = \frac{\Delta x}{\Delta t}$$

$$\frac{60\text{miles}}{\text{hour}} = \frac{200\text{miles}}{\Delta t}$$

$$60\text{miles}(\Delta t) = 200\text{miles} \cdot \text{hour}$$

$$\Delta t = \frac{200\text{miles} \cdot \text{hour}}{60\text{miles}} = 3.33\text{hours}$$

3. You drop a rock off of a very high bridge. The rock accelerates at a rate of -9.8m/s^2 . You see a splash 8 seconds after you release the rock. What is the rock's velocity when it hits the water?

$$a = -9.8\text{m/s}^2$$

$$\Delta t = 8\text{s}$$

$$\bar{a} = \frac{\Delta v}{\Delta t}$$

$$-9.8\text{m/s}^2 = \frac{\Delta v}{8\text{s}}$$

$$\Delta v = (-9.8\text{m/s}^2)(8\text{s}) = -78.4\text{m/s}$$

$$\Delta v = ?$$

4. A ball falls for 10 seconds with an acceleration of -9.8m/s^2 . What is the ball's displacement during this time?

$$\Delta t = 10\text{s}$$

$$a = -9.8\text{m/s}^2$$

$$V_{x0} = 0\text{m/s}$$

$$\Delta x = ?$$

$$\Delta x = V_{x0}t + \frac{1}{2}at^2$$

$$\Delta x = (0\text{m/s})(t) + \frac{1}{2}(-9.8\text{m/s}^2)(10\text{s})^2$$

$$\Delta x = -490\text{m}$$

5. A runner's velocity at 12:34:33 PM is 4m/s. At time 12:34:38 PM, the runner's velocity is 2m/s. What is the runner's average acceleration over this time period?

$$\Delta t = 5s$$

$$\Delta v = -2m/s$$

$$\bar{a} = \frac{\Delta v}{\Delta t} = \frac{-2m/s}{5s} = -0.4m/s^2$$

8. A child traveling at a rate of -15m/s along a zip line. After decelerating at a constant rate for 5 seconds, the child comes to a stop.

- a. What is the child's average acceleration?

$$v_{x0} = -15m/s \quad v_x = v_{x0} + at$$

$$\Delta t = 5s$$

$$v_x = 0m/s$$

$$0m/s = -15m/s + a(5s)$$

$$15m/s = a(5s)$$

$$\frac{15m/s}{5s} = a$$

$$3m/s^2 = a$$

- b. What distance does the child travel during this deceleration period?

$$a = 3m/s^2 \quad \Delta x = v_{x0}t + \frac{1}{2}at^2$$

$$\Delta t = 5s$$

$$v_{x0} = -15m/s$$

$$v_x = 0m/s$$

$$\Delta x = (-15m/s)5s + \frac{1}{2}(3m/s^2)(5s)^2$$

$$\Delta x = -75m + \left(\frac{3}{2}m/s^2\right)(25s^2)$$

$$\Delta x = -75m + 37.5m = -37.5m$$

9. A driver sees a turtle in the road and hits the brakes. It takes him 3 seconds to stop, and the car slides a distance of 20 meters. What was his car's rate of deceleration?

$$\Delta x = 20m$$

$$\Delta t = 3s$$

$$v_x = 0m/s$$

$$\Delta a = ?$$

$$v_{x0} = 13.3m/s$$

$$a = \frac{\Delta v}{\Delta t} = \frac{v_x - v_{x0}}{\Delta t} = \frac{0m/s - 13.3m/s}{3s} = \frac{-13.3m/s}{3s} = -4.4m/s^2$$

10. How fast was the driver (from the previous question) going before he hit the brakes?

$$\Delta x = 20m$$

$$\Delta t = 3s$$

$$v_x = 0m/s$$

$$v_{x0} = ?$$

$$\bar{v} = \frac{v_{x0} + v_x}{2} = \frac{\Delta x}{\Delta t}$$

$$\frac{v_{x0} + 0m/s}{2} = \frac{20m}{3s}$$

$$v_{x0} = \frac{40m}{3s} = 13.3m/s$$