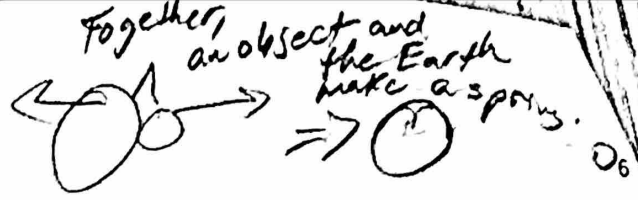


Together, an object and the Earth make a spring. 

Work and Power Practice:

$W = 588N$

3. A 60kg student climbs 12m up a vertical rock wall in 50 seconds. The student's speed is constant.

a. Approximately how much work did the student do?
 $W = Fd = 588N(12m) = 7056J$
 $F = \text{weight} = 60kg(9.8m/s^2) = 588N$

b. What was the student's average power output, in Watts?

$P = \frac{W}{t} = \frac{7056J}{50s} = 141W$

c. How long would the climb have taken if the student's power output had been 1 horsepower?

$1hp = 746W \Rightarrow P = \frac{W}{t} \Rightarrow 746W = \frac{7056J}{t} \Rightarrow t = 9.46s$

d*. Just for fun, contemplate the amount of work done on the student.

$a = 0 \Rightarrow \Sigma F = 0 \quad W = 0(12m) = 0J \quad \Delta KE = 0 \Rightarrow W = 0$

4. When a 0.5kg water rocket is launching, the rocket's thrust (technically the push of the water) exerts a 400N upward force on the rocket over a vertical distance of 1m. By how much do the rocket's PE and KE change over this time?

$PE_0 + KE_0 + W_{nc} = PE + KE$
 $0 + 0 + 400N(1m) = 0.5kg(9.8m/s^2)(1m) + KE$
 $400J = 4.9J + KE \Rightarrow KE = 395.1J$
They gain this much

6. Assuming that the rocket from #5 started from rest, use the KE formula to find the rocket's velocity after accelerating for that one meter.

$KE = \frac{1}{2}mv^2 \Rightarrow 395.1J = \frac{1}{2}(0.5kg)(v^2)$
 $v = 39.8m/s$

7. A 2kg package is sliding across a surface with a velocity of 3m/s. The force of friction acting on the package is 1N. How far will the package slide before it stops?

$PE_0 + KE_0 + W_{nc} = PE + KE$
 $0J + \frac{1}{2}(2kg)(3m/s)^2 + F_f d = 0 + 0 \Rightarrow 9J - 1N(d) = 0$
 $d = 9m$

Potential Energy Practice:

7. A 3kg watermelon is dropped from a height of 100m. What is its potential energy at its release point (100m)?

$PE = mgh = 3kg(9.8m/s^2)(100m) = 2940J$

8. What is the watermelon's potential energy when it has fallen to an altitude of 25m?

$PE = 3kg(9.8m/s^2)(25m) = 735J$

9. What is the watermelon's KE when its altitude is 25m?

$PE_0 + KE_0 = PE + KE$
 $2940J + 0 = 735J + KE \Rightarrow KE = 2205J$

No friction

10. What is the watermelon's velocity when its altitude is 25m?

$KE = \frac{1}{2}mv^2 \quad 2205J = \frac{1}{2}(3kg)(v^2)$
 $v = 38.3m/s$

11. A 20kg child sits at rest at the top of a slide which is 5m long and 3m high. As the child slides down the slide, the child experiences a constant 5N force of friction.

a. What is the child's total energy at the top of the slide? What form of energy does the child have?

$$PE = \frac{1}{2} (20\text{kg}) (9.8\text{m/s}^2) (3\text{m}) = 588\text{J} = PE$$

b. How much work is done by friction?

$$W = Fd = -5\text{N} (5\text{m}) = -25\text{J}$$

c. How much PE and KE does the child have at the bottom of the slide?

$$PE_0 + KE_0 + W_{nc} = PE + KE$$

$$588\text{J} + 0 - 25\text{J} = 0 + KE \rightarrow KE = 563\text{J}$$

d. What is the child's speed upon reaching the bottom of the slide?

$$563\text{J} = \frac{1}{2} (20\text{kg}) v^2 \Rightarrow v = 7.5\text{m/s}$$

Other Energy Units: 1 Joule is derived from the amount of energy required to raise 1kg of water by 1°C. 1calorie = 4.184 Joules. 1 "food calorie" = 1kcal = 1,000 calories = 4,184 Joules. The "calories" used to describe nutrition values are actually kilocalories.

Work and Energy Practice Problems:

- A stick pushes a 170g hockey puck with a constant force of 100N over a distance of 0.4m and a time of 0.1 seconds.
 - How much work is done on the puck?
 - How much power does the stick use while it is pushing the puck?
 - Assuming that the puck starts from rest, what is its speed after being pushed by the stick?
- A dad pulls his daughter in a sled. He drags the sled using a long rope, which is essentially horizontal, maintaining a constant tension of 100N.
 - How much work does the dad do if he pulls his daughter for one mile?
 - A Snickers Bar contains about 260,000 calories of energy. Assuming that the dad's body is 30% efficient (makes use of only 30% of its energy intake), how many Snickers bars must he eat to replace the energy lost by dragging his daughter around?
- A 5kg bowling ball is hanging by a cable from the ceiling of a train. The cable makes a 70° angle with the ceiling. During a certain time interval, the train travels 30m.
 - What is the horizontal component of the tension in the cable?
 - How much net work is done on the ball during this time interval?
 - If the velocity of the train and ball were both 10m/s at the beginning of this time interval, what are their velocities at the end of the time interval?
- Suppose it takes 100J of energy to smash an apple. What horsepower is required to smash 5 apples in 1 seconds?