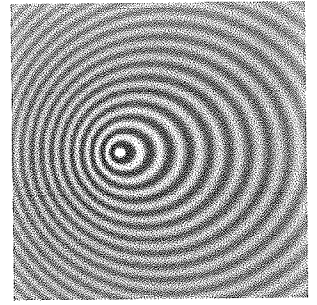


Name: Key

Practice 17.4 - Doppler Effect



Equations:

$$v = 331.3 \sqrt{1 + \frac{T}{273.15}} \approx 331.3 + 0.606 T \text{ m/s}$$

$$f_o = f_s \frac{v \pm v_o}{v \pm v_s}$$

1. Suppose a train that has a 150-Hz horn is moving at 35.0 m/s in still air on a day when the speed of sound is 340 m/s.

A. What frequencies are observed by a stationary person at the side of the tracks as the train approaches and after it passes?

Approaching: $f_o = (150 \text{ Hz}) \frac{340 \frac{\text{m}}{\text{s}}}{340 - 35.0 \frac{\text{m}}{\text{s}}} = \boxed{167 \text{ Hz}}$

Receding: $f_o = (150 \text{ Hz}) \frac{340 \frac{\text{m}}{\text{s}}}{340 + 35.0 \frac{\text{m}}{\text{s}}} = \boxed{136 \text{ Hz}}$

B. What frequency is observed by the train's engineer traveling on the train?

$\boxed{150 \text{ Hz}}$ There is no relative motion between the horn & the engineer.

2. What frequency is received by a mouse just before being dispatched by a hawk flying at it at 25.0 m/s and emitting a screech of frequency 3500 Hz? Take the speed of sound to be 331 m/s.

Hawk is approaching $\Rightarrow f_o = (3500 \text{ Hz}) \frac{331 \frac{\text{m}}{\text{s}}}{331 - 25.0 \frac{\text{m}}{\text{s}}} = \boxed{3.79 \times 10^3 \text{ Hz}}$

3. A car passes through an intersection at $1.00 \times 10^2 \text{ km/hr}$. If the air temperature is 20.0°C and the frequency of the car's horn is $3.00 \times 10^2 \text{ Hz}$, what change in frequency would a stationary observer notice as the car passes? Note: $\Delta f = f_{\text{towards}} - f_{\text{away}}$

$$v = 331.3 \sqrt{1 + \frac{20.0^\circ\text{C}}{273.15}} = 343.2 \frac{\text{m}}{\text{s}} \quad 100 \frac{\text{km}}{\text{h}} \left(\frac{1 \text{ h}}{3600 \text{ s}} \right) \left(\frac{1000 \text{ m}}{1 \text{ km}} \right) = 27.78 \frac{\text{m}}{\text{s}}$$

Towards: $f_o = (3.00 \times 10^2 \text{ Hz}) \frac{343.2 \frac{\text{m}}{\text{s}}}{343.2 - 27.78 \frac{\text{m}}{\text{s}}} = 326.4 \text{ Hz}$

Away: $f_o = (3.00 \times 10^2 \text{ Hz}) \frac{343.2 \frac{\text{m}}{\text{s}}}{343.2 + 27.78 \frac{\text{m}}{\text{s}}} = 277.5 \text{ Hz}$

$$\Delta f = \boxed{48.9 \text{ Hz}}$$

4. Two police cars pass each other, both moving at 80.0 km/hr. The air temperature is 25.0 °C. If each car sounds its siren with a frequency 4.00×10^2 Hz, what change in frequency will be heard by each policeman as the cars pass?

$$V = 331.3 \sqrt{1 + \frac{25.0}{273.15}} = 346.1 \frac{\text{m}}{\text{s}} \quad 80 \frac{\text{km}}{\text{h}} \left(\frac{1 \text{ h}}{3600} \right) \left(\frac{1000 \text{ m}}{1 \text{ km}} \right) = 22.22 \frac{\text{m}}{\text{s}}$$

$$\text{Toward: } f_o = 400 \text{ Hz} \left(\frac{346.1 + 22.22 \frac{\text{m}}{\text{s}}}{346.1 - 22.22 \frac{\text{m}}{\text{s}}} \right) = 454.9 \text{ Hz} \quad \Delta f = \boxed{103 \text{ Hz}}$$

$$\text{Away: } f_o = 400 \text{ Hz} \left(\frac{346.1 - 22.22 \frac{\text{m}}{\text{s}}}{346.1 + 22.22 \frac{\text{m}}{\text{s}}} \right) = 351.7 \text{ Hz}$$

5. A sound meter at a race track records the frequency of the exhaust of an approaching race car to be 6.00×10^2 Hz. The actual frequency is known to be 5.30×10^2 Hz. The air temperature is 20.0 °C. How fast is the car going?

$$V = 331.3 \sqrt{1 + \frac{20.0}{273.15}} = 343.2 \frac{\text{m}}{\text{s}}$$

$$f_o = f_s \frac{V}{V - V_s} \Rightarrow \frac{f_o}{f_s} = \frac{V}{V - V_s} \Rightarrow V - V_s = \frac{V}{f_o/f_s} \Rightarrow V_s = V - \frac{V}{f_o/f_s}$$

$$V_s = V \left(1 - \frac{f_s}{f_o} \right) = 343.2 \left(1 - \frac{530}{600} \right) = \boxed{40.0 \frac{\text{m}}{\text{s}}}$$

6. A sound meter records the exhaust frequency of a receding race car to be 4.00×10^2 Hz. The actual frequency is 4.50×10^2 Hz. If the air temperature is 15.0 °C, how fast is the car going?

$$V = 331.3 \sqrt{1 + \frac{15.0}{273.15}} = 340.3 \frac{\text{m}}{\text{s}}$$

$$f_o = f_s \frac{V}{V + V_s} \Rightarrow V + V_s = \frac{V}{f_o/f_s} \Rightarrow V_s = V \left(\frac{f_s}{f_o} - 1 \right)$$

$$V_s = 340.3 \frac{\text{m}}{\text{s}} \left(\frac{450}{400} - 1 \right) = \boxed{42.5 \frac{\text{m}}{\text{s}}}$$